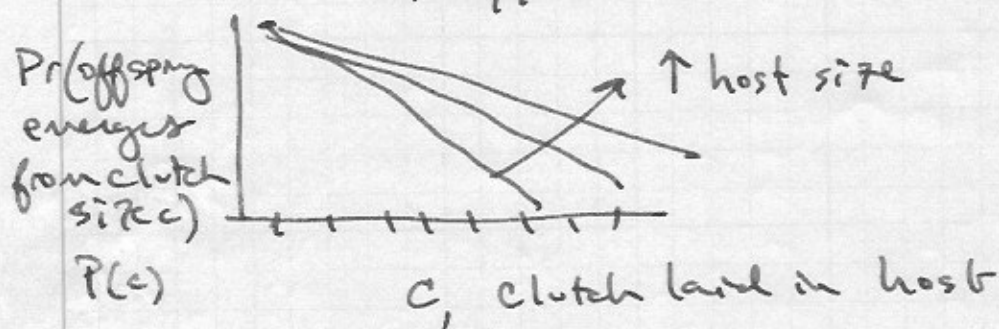


16.1

## Canonical Equation for Allocation Processes

- (A) { - Pro-oviger ~ insect emerges w/ all eggs viable  
 - Syn-oviger ~ mother through life  
 (B) { - Solitary - one egg per host  
 - Gregarious - many eggs per host

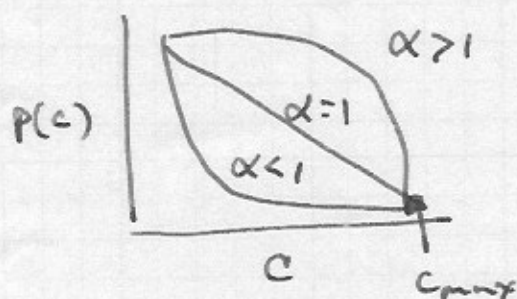
- Hosts come in various sizes
- Chance that offspring survives ~~by~~ best declines w/ eggs laid



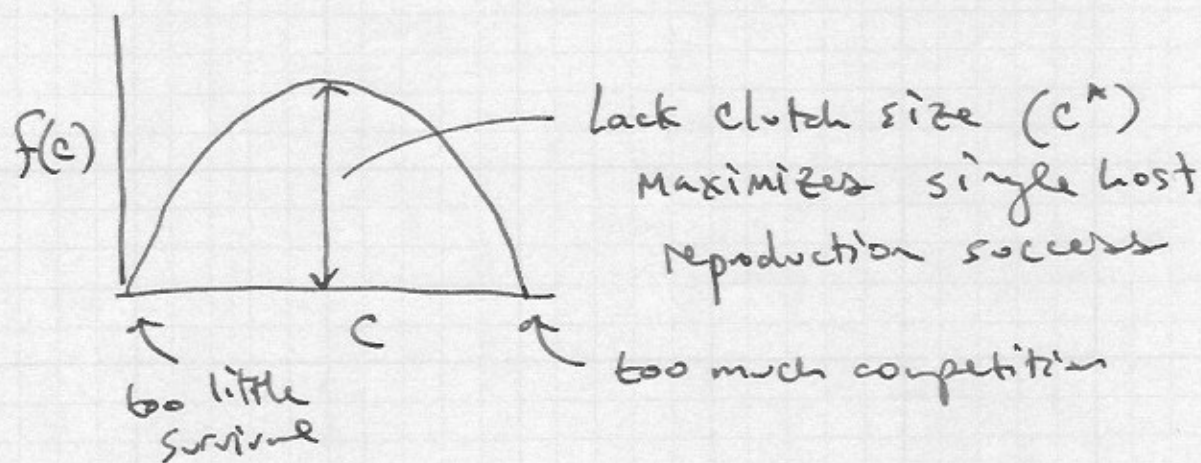
Model for  $p(c)$

$$p(c) = S_0 \left[ 1 - \left( \frac{c-1}{c_{max}-1} \right)^\alpha \right]$$

$$S_0 \sim p \leq S_0 \leq 1$$



$$\begin{aligned}
 f(c) &= E \{ \# \text{ of offspring emerging from clutch of} \\
 &\quad \text{size } c \} \\
 &= c p(c)
 \end{aligned}$$



- A parasite is born with  $X$  eggs
  - encounters only one kind of host
  - lack clutch size is  $c^*$
  - If parasitoid were guaranteed life until all eggs are laid, optimal clutch size is  $1/\text{host}$

$\mu_s$  = mortality rate while searching for host  
 $\mu_c$  = mortality rate when  $c$  eggs are laid in a host

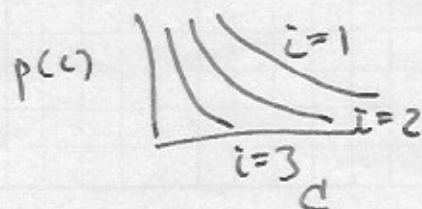
$$\text{Pr}(\text{female survives one unit of search}) = e^{-\mu_s}$$

$$\text{Pr}(\text{female survives laying a clutch of size } c) = e^{-\mu(c)}$$

$$0 \leq \mu_s \leq \infty$$

$$0 \leq \mu(c) \leq \infty$$

Consider multiple host types, of type  $i$



$\lambda_i$  = prob finding host  $i$   
 $1 - \sum \lambda_i$  = prob of no encounter

16.3  $X(t)$  = egg complement @  $t$

$T$  = time of first frost

- if female egg number is held constant,  
clutch size  $\uparrow$  as  $t \rightarrow T$

$F(x, t)$  = maximum expected accumulated offspring  
production btw  $t + T$  given egg complement  
is  $X(t) = x$

$$F(x, T) = 0$$

~~$X(t)$  = egg complement @  $t$~~

~~$F(x, t)$  = max.~~

$$F(x, t) = (1 - \sum \lambda_i) e^{-\mu s - 1} F(x, t+1) \\ + e^{-\mu s - 1} \sum_{i=1}^I \lambda_i \max_c \left\{ f_i(c) + e^{-\nu(c)} F(x-c, t+c+t_a) \right\}$$

No encounter survives (no change in egg comp.)

⊛  $\mu(c) = \mu_0 \cdot c$  mortality for laying one egg  
rate  $t_a$  = time it takes to access host

⊛ Maximization results in  $c^*(x, i, t)$   
= optimal clutch size for individual given  
host type  $i$  @ time  $t$  when ♀ has  $x$  eggs

as  $\mu_0 \uparrow$ ,  $e^{-\mu_0 c} \downarrow$ , which  $\downarrow$  future fitness  
and  $\uparrow f(c)$   
reliability

i.e. less likely you will survive  $\downarrow$ , so consent  
fitness more important, so expect  $\uparrow$  clutch  
size for  $\uparrow \mu_0$